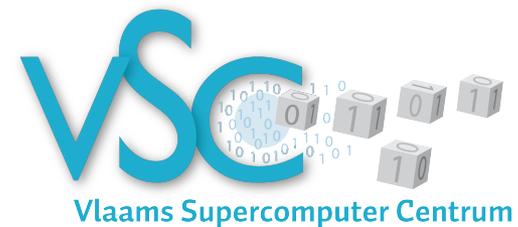


HPC TNT - 2

Tips and tricks for **Vectorization approaches to efficient code**

HPC core facility CalcUA



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- Introduction
 - What is vectorization
 - Why does it matter
 - When does it not matter
- Different approaches
- Case study – magnetization
- Final remarks

- Focus of this talk is on big picture and background not on the details

What is vectorization

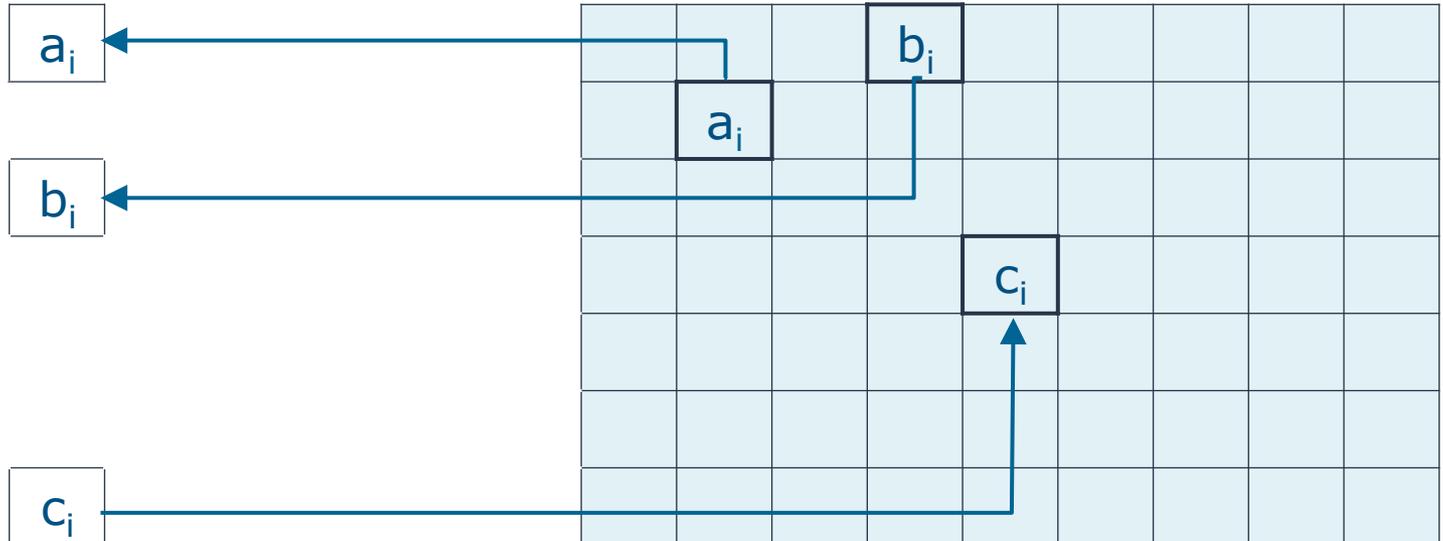
```
do i=1,n
  c(i) = a(i)+b(i)
end do
```

instr.

registers

main memory or cache

load a_i



load b_i



add

store c_i

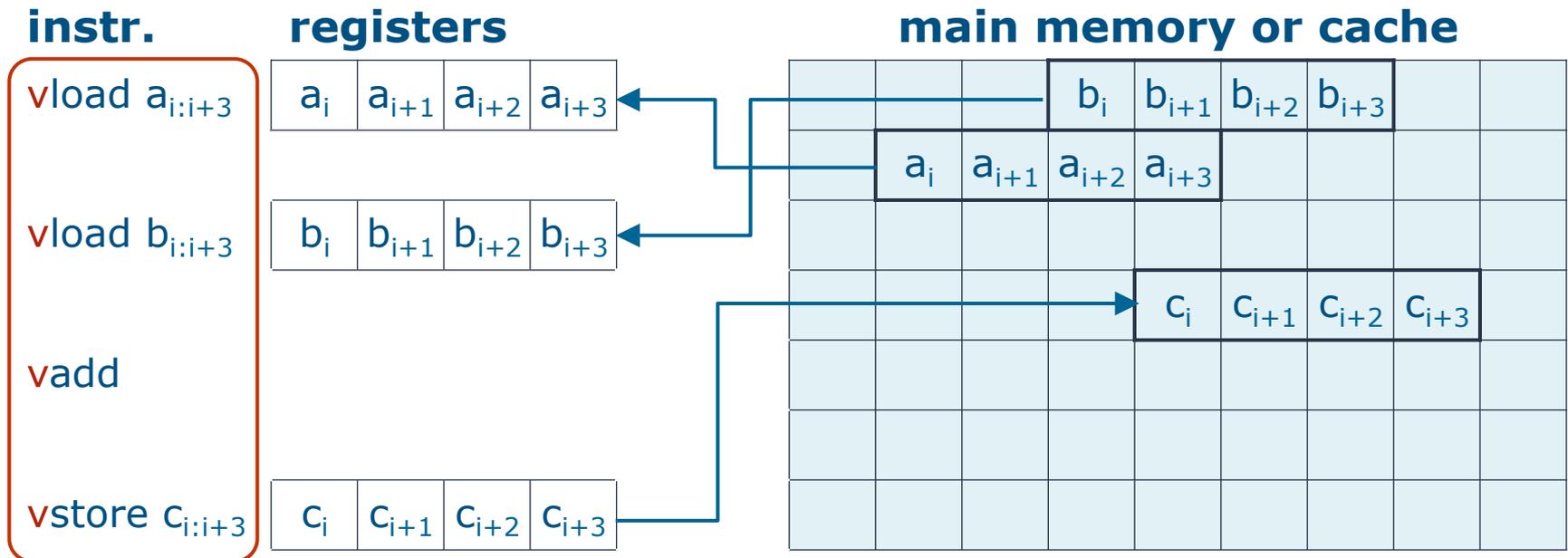


What is vectorization

```
do i=1,n,4
  c(i:i+3) = a(i:i+3)+b(i:i+3)
end do
```

Vector width

SIMD
Single Instruction
Multiple data



Vector instructions

Cpu	Instruction set	Vector width	Vector width SP	Vector width DP
Westmere	SSE4.2	128 bit	4	2
Ivy bridge	AVX	256 bit	8	4
Haswell	AVX2	256 bit	8	4
Xeon Phi	AVX-512	512 bit	16	8

Hopper

Failing to vectorize implies that your application runs **at best** at no more than 25% (12.5%) of peak performance for DP (SP)

when not to focus on vectorization (yet)

```
do i=1,n,4
  c(i:i+3) = a(i:i+3)+b(i:i+3)
end do
```

instr.

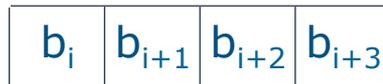
registers

<- 250 cycles main memory
<- 1 cycle cache

vload $a_{i:i+3}$

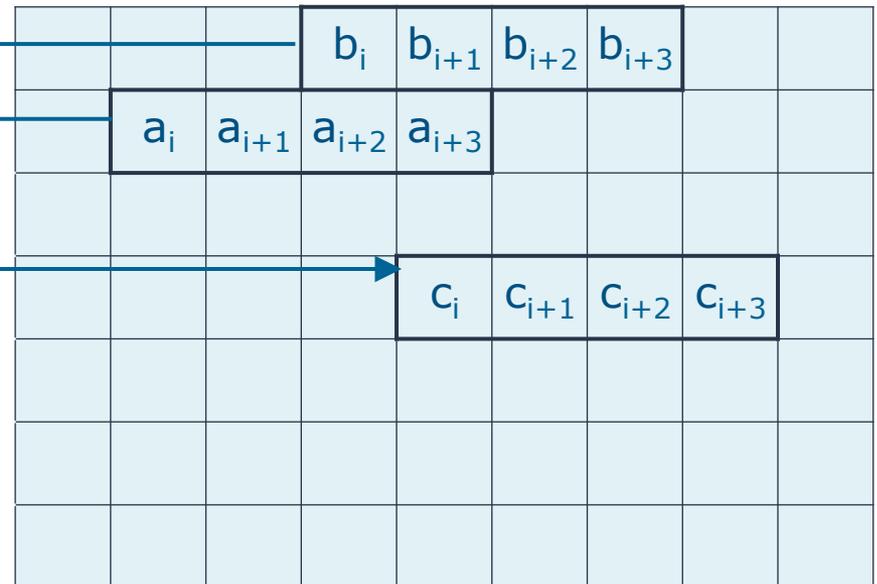


vload $b_{i:i+3}$



vadd

vstore $c_{i:i+3}$



When not to focus on vectorization (yet)

- Application with slow data traffic: every item needs to be fetched from main memory or from another node
 - Reorganize data layout
 - Sort data in the order the application needs them
- use PerfExpert on Hopper to find out about data traffic problems

Organize data

State of all persons

List of ill people

List of healthy people

```
do i=1,n_ill:
  do j=1,n_healthy
    if contaminate(
      persons(ill(i)),
      persons(healthy(j)))
      move_to_ill(healthy(j))
    end do
  end do
end do
```

State of ill people

State of healthy people

```
do i=1,n_ill:
  do j=1,n_healthy
    if contaminate(
      ill_persons(i),
      healthy_persons(j))
      move_to_ill(healthy_persons(j))
    end do
  end do
end do
```

When not to focus on vectorization (yet)

- Application saturates bandwidth
 - The bottleneck is not computation
 - Try to do all possible work on data when it is in cache (blocking/tiling)
 - If there is not much to compute vectorization will not help
- use PerfExpert on Hopper to find out

Blocking/tiling

```
// inefficient // efficient
// except small problems // chunk = collection of items
//                               // that fits in L1 cache

For all items                    For all chunks
  Do this                        For all items in chunk
For all items                    Do this
  Do that                        For all items in chunk
For all items                    Do that
  Do something else              For all items in chunk
                                  Do something else

// data transferred 3x          // data transferred once
```

Approaches to vectorization

- Assembly code
- Intrinsic
- Auto-vectorization by compiler
 - GCC
 - Intel compiler suite
- low level library
 - boost.simd
 - Vc
 - Intel Cilk++
- optimized high level library
 - Eigen
 - Intel MKL

- Write assembly code that use SIMD instructions (SSE, AVX, ...)

```
for (int i = 0; i<N; ++i) C[i] = A[i] + B[i];
```

V=AVX, mov=move, u=unaligned, p=packed, s=single precision

NEXT ITERATION:

```

vmovups ymm1, ymmword ptr [edi+edx*4+8] ; copy 32 bytes from B to ymm1
vmovups ymm0, ymmword ptr [esi+edx*4+8] ; copy 32 bytes from B to ymm1
vaddps ymm1, ymm1, ymm0; add ymm0 to ymm1 and store the result in ymm1
vmovups ymmword ptr [ecx+edx*4+8], ymm1; copy 32 bytes from ymm1 to C
add edx, 8 ; increase loop index by 8
cmp edx, dword ptr [esi+4]
jg NEXT_ITERATION
  
```

- Layer of data types and functions made available by compiler through **include file** (C/C++)

```
#include <immintrin.h>
```

```
...
```

```
__m256 ymm0, ymm1; //define the vector registers used
```

```
float a[8]={1,2,3,4,5,6,7,8};
```

```
float b[8]={2,3,4,5,6,7,8,9};
```

```
float c[8];
```

```
ymm0 = __builtin_ia32_loadups256(a); // ymm0 <= a
```

```
ymm1 = __builtin_ia32_loadups256(b); // ymm1 <= b
```

```
ymm0 = __builtin_ia32_mulps256(ymm0, ymm1); // ymm0 <= ymm0*ymm1
```

```
__builtin_ia32_storeups256(c, ymm0); // c <= ymm0
```

```
...
```

Approaches to vectorization assembly/intrinsics

assembly

Pro

- Can be very efficient

Con

- Hard, tedious, error-prone
- Depend on hardware
- Low level

intrinsics

- Can be very efficient
- Stay in the language

- Only slightly less hard
- Depend on hardware and on compiler
- Only C/C++

Approaches to vectorization

3. Auto-vectorization

- the compiler is your friend - let the compiler handle it
- number of constraints
- you can help the compiler
 - Compiler directives
 - Language extensions (`restrict`)

Pro

- usually efficient
- relatively easy

Con

- depend (only) on compiler

- Constraints
 - inner loop only
 - loop count must be known in advance
 - single entry, single exit (no break)
 - no I/O
 - no branches (but you can use masks)
 - only intrinsic math functions and
 - C/C++ inlined functions, with no side effects
 - Fortran elemental functions
 - each iteration must be independent
 - $a(i) = a(i-4) + b(i)$ is ok with vector length 2, **not** 4

Approaches to vectorization

auto-vectorization

- If the compiler cannot unambiguously decide that there is no dependency, the loop is not vectorized

Mind pointers in C/C++/Fortran!

```
double sum(double* a, double* b, double* c, int N) {
    double ab=0;
    for( int i=0; i<N; ++i ) c[i]=a[i]+b[i-2]
}
```

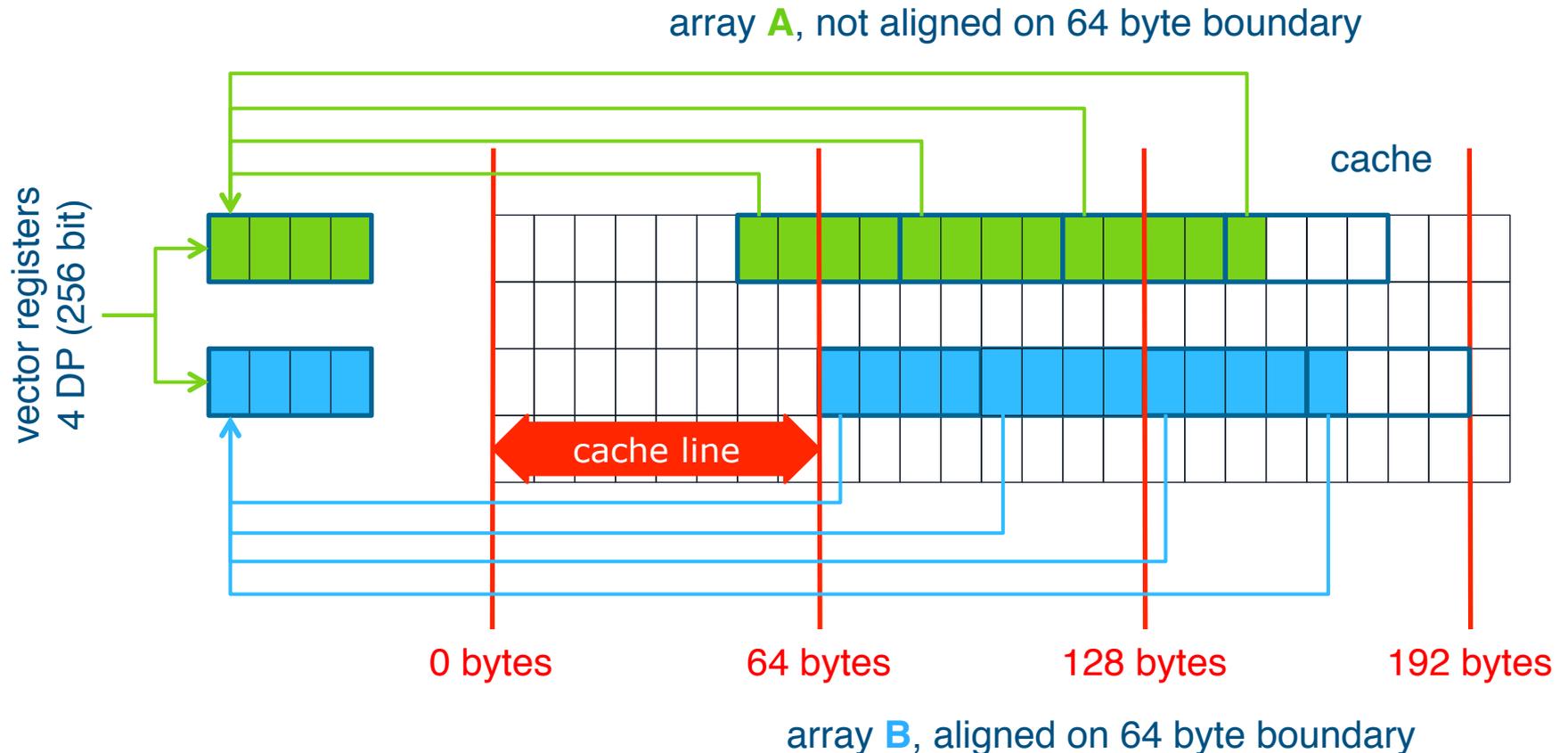
is not vectorized:

c may be an alias for b -> **assumed dependency**

```
double sum(double* restrict a, double* restrict b,
           double* restrict c, int N) {
    double ab=0;
    for( int i=0; i<N; ++i ) c[i]=a[i]+b[i-2]
}
```

- Fortran has arrays, C/C++ does not: double a[] is pointer too!

alignment issues - 1



- alignment of arrays on 64 byte boundary can have important performance effect
- increased pressure on prefetcher (every second vector comes from 2 cache lines)

alignment of static arrays

- linux C/C++

```
float A[1000] __attribute__((aligned(64)));
```

- Fortran

```
real :: A(1000)  
!dir$ attributes align: 64:: A
```

alignment of dynamic/allocatable arrays

- linux C/C++ (unfortunately not very elegant)
 - operator new cannot handle alignment
 - replace malloc and free with `_mm_malloc` and `_mm_free` [intel compiler only]
 - Use of `std::_aligned_malloc` and placement new
 - <http://cottonvibes.blogspot.be/2011/01/dynamically-allocate-aligned-memory.html>
 - Intel TBB provides a **portable** `cache_aligned_allocator`
- still must inform the compiler on alignment

```

void myfun( double *a, int n) {
    __assume_aligned(a, 64);
    for( int j=0; j<n; ++j )
        ++a[j];
}
  
```

alignment of dynamic/allocatable arrays

- Fortran

```
real, allocatable :: a(:)
!dir$ attributes align:64 :: a
```

- still must inform the compiler on alignment

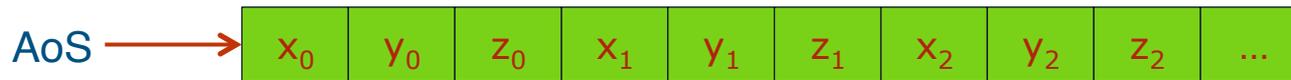
```
!DIR$ ASSUME_ALIGNED A: 64
```

```
...
```

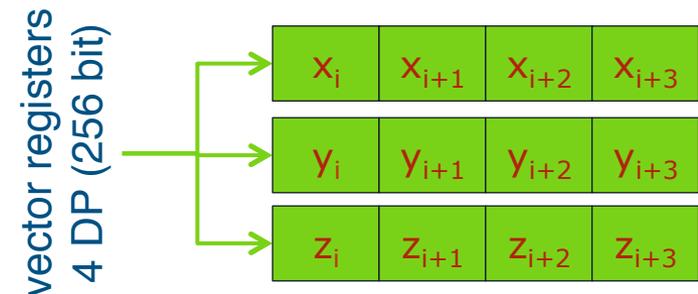
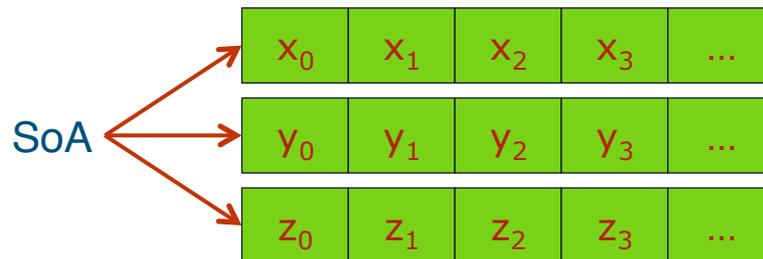
```
do i=1, N
  A(I) = A(I) + 1
end do
```

alignment issues - 2

- compute norm of vector : $\sqrt{x_i^2 + y_i^2 + z_i^2}$
- AoS: a single array containing (x, y, z) triplets



- SoA: separate array for x , y and z values



- SoA: vector registers can be filled with contiguous memory = as efficient as it can get
- AoS: vector registers must be filled by gathering noncontiguous elements

- Compiler can provide vectorization report
- Intel <15.0: `-vec-report[=n]`
 - `n=0` no report
 - `n=1` report vectorized loops
 - `n=2` report vectorized and non-vectorized loops
 - `n=3` 2+report proven or assumed dependencies
 - `n=4` report non-vectorized loops
 - `n=5` 4+reason why not
- Intel ≥ 15.0 : `-qopt-report[=n]`
 - Generate optimisation report
 - `n=0..5` increasing detail
- Use report to understand and improve auto-vectorization

Approaches to vectorization

auto-vectorization

- Use compiler directives to help the compiler
 - Fortran `!DEC$ directive`
 - C/C++ `#pragma directive`
 - `ivdep` Instructs the compiler to ignore assumed vector dependencies (but not proven ones)
 - `vector {aligned|unaligned|always|temporal|nontemporal}` Specifies how to vectorize the loop and indicates that efficiency heuristics should be ignored. Using the `assert` keyword with the `vector {always}` pragma generates an error-level assertion message saying that the compiler efficiency heuristics indicate that the loop cannot be vectorized. Use `#pragma ivdep!` to ignore the assumed dependencies.
 - `novector` Specifies that the loop should never be vectorized.
 - `simd` Enforces vectorization of loops.

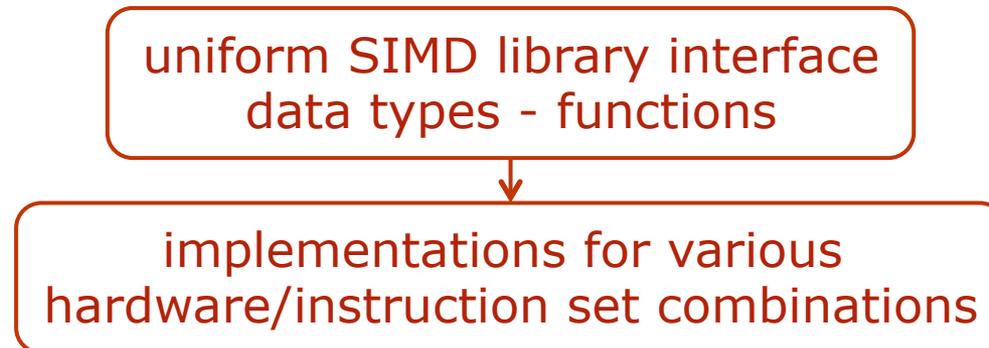
Approaches to vectorization auto-vectorization

- Use compiler directives with care!
 - Assert that ignoring assumed dependencies are actually non happening
- Compiler flags to force these directives application wide
Use with even greater care!
- GCC has auto-vectorization, but Intel compiler should be your first choice

Approaches to vectorization

4. Low level libraries

- “architecture independent intrinsics”



- The compiler translates the generic data types and operator/function calls into assembly instructions

Approaches to vectorization

4. Low level libraries

- code can be compiled to
 - run even in the absence of SIMD hardware
 - select most efficient implementation available automatically at runtime!
- handle alignment requirements
- ideal for implementation of high level libraries
- **boost.simd** is component of NT² Numerical Template Toolbox (not part of boost (yet?):
 - github.com/MetaScale/nt2
- **Vc** is found at gitorious.org/vc
- Intel Cilk++

Approaches to vectorization low level libraries

Pro

- Efficient
- Easy
- Flexible

Con

- Depend on library
(Boost.simd and Vc are interesting but small initiatives, support may stop at some point)
- Only C/C++
(afaik)
- Low level
(but higher than intrinsics)

Approaches to vectorization

5. high level libraries

- Formulate your problem in terms of library calls
- Trust that library designers have done good job
- E.g. Intel MKL, Eigen, ...

Pro

- Low development cost
- Little coding/debugging/maintenance
- Focus on problem

Con

- Depend on library
- No competitive edge
- Not so flexible

	stay away		preferred choice		preferred choice
	assembly	intrinsic	auto-vect	low lvl lib	high lvl lib
efficiency	++	++	++	++	+
easy to use	--	-	+	+	++
flexibility	++	++	++	++	-
dependency	hardware	hardware Compiler	compiler	lib	lib
portability	-	-	+	++	++
language	F90/C/C++	C/C++	F90/C/C++	C/C++ if portability is an issue and software is first concern	F90/C/C++ if solving the problem is first concern

where to look for the details

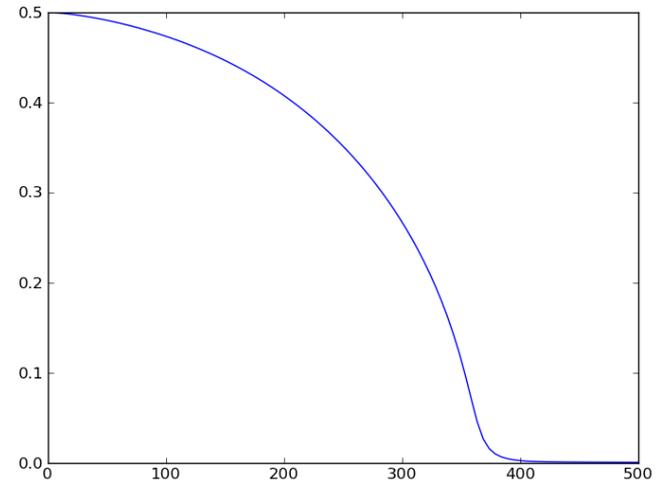
- **<https://software.intel.com/en-us/intel-software-technical-documentation>**
- <https://software.intel.com/sites/default/files/8c/a9/CompilerAutovectorizationGuide.pdf>
- https://software.intel.com/en-us/mkl_cookbook
- <https://software.intel.com/en-us/articles/vectorization-essential>

spin-waves-2.0

Prof Wim Magnus

CASE STUDY

- compute magnetization $m(T)$ of bulk ferro-magnets



- self consistent solution of

$$m = \frac{1}{2} \cdot \frac{1}{1 + 2\Phi(m)}, \quad \Phi(m) = \frac{1}{N} \sum_{\mathbf{k}} \frac{1}{e^{\beta\eta(\mathbf{k})m} - 1},$$

$$\beta = 1/k_B T$$

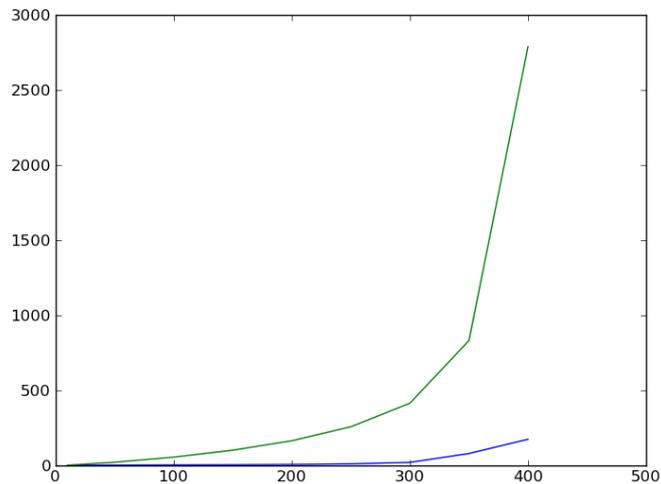
- loop over all T points (temperature)
 - initial guess $m=0.5$ (corresponding to $\Phi(m)=0$)
 - update $m = 1/(2+4*\Phi(m))$ until convergence

- $\Phi(m)$ is computed as

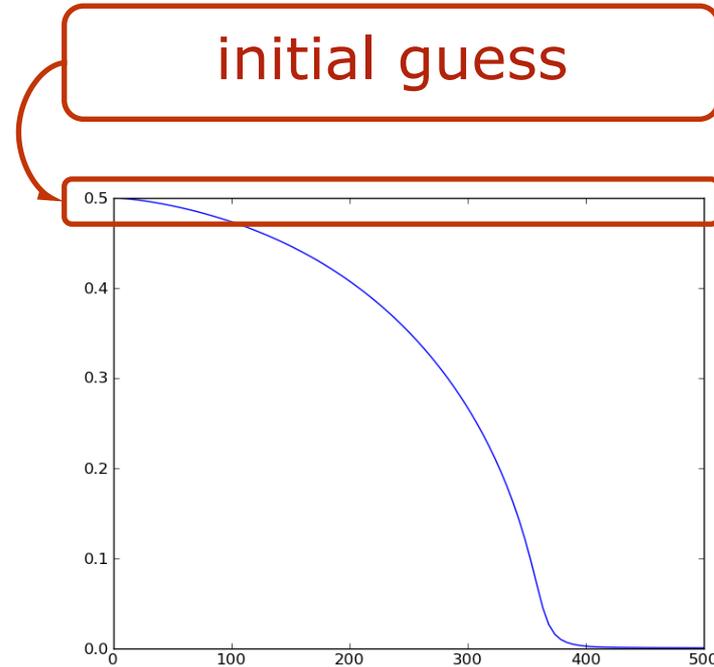
$$\Phi(m) = \sum_{n=1}^{\infty} \left(\frac{a}{\pi} \int_0^{\pi/a} dq e^{-nm\beta\eta_1(q)} \right)^3$$

- $\Phi(m)=0$
- loop over $n=1, \infty$
 - evaluate the integral using Gauss-Legendre-integratie on 64 points
 - term = (integral* a/π)³
 - if the term is too small
 - break
 - else
 - $\Phi(m)+=term$

- 4 nested loops:
- loop over T points
 - self-consistency iteration
 - loop over terms
 - loop over integration points
- observation:
runtime does not increase when auto-vectorization is disabled with compiler flag
 - `-no-vec`
- auto-vectorization fails, but why?

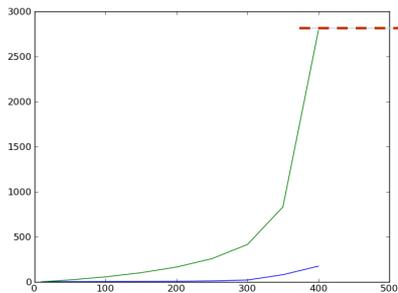


- number of iterations in self-consistency loop vs T



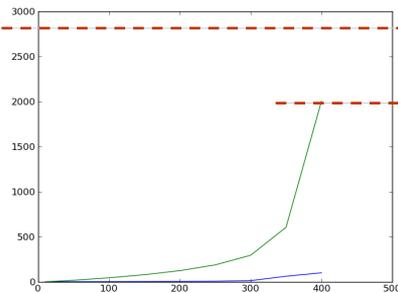
- $m(T)$ decreases monotonically
- $m(T_{i-1})$ is a better initial guess than 0.5

think about your problem when you code



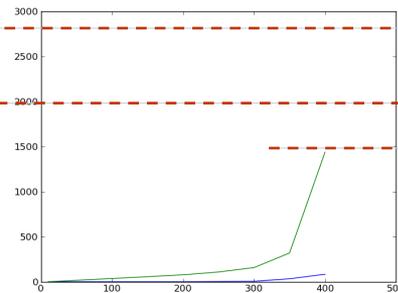
$$m_0(T_i) = 0.5$$

2789



$$m_0(T_i) = m(T_{i-1})$$

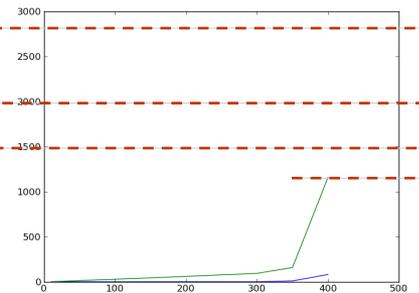
2789->2005



$$m_0(T_i) =$$

linear
interpolation
 $m(T_{i-1}), m(T_{i-2})$

2005->1439



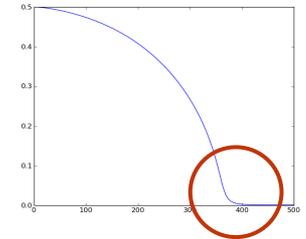
$$m_0(T_i) =$$

quadratic
interpolation
 $m(T_{i-1}), m(T_{i-2}),$
 $m(T_{i-3})$

1439->1157

2789->1157 is roughly a speed up of 2.4

- original code takes about 11 s to run
- 0.58 s is spent writing warnings to stdout
- when $m \rightarrow 0$ there are problems with convergence of



- the series

$$\Phi(m) = \sum_{n=1}^{\infty} \left(\frac{a}{\pi} \int_0^{\pi/a} dq e^{-nm\beta\eta_1(q)} \right)^3$$

- and the self-consistency loop

$$m = \frac{1}{2} \cdot \frac{1}{1 + 2\Phi(m)}$$

- I/O is expensive – don't write what you will never read
- hundreds of times the same two warnings, better use a counter and report only once

$$\Phi(m) = \sum_{n=1}^{\infty} \left(\frac{a}{\pi} \int_0^{\pi/a} dq e^{-nm\beta\eta_1(q)} \right)^3$$

- Gauss-Legendre integration implemented using allocatable array for integration points
- the integrand is passed as function pointer
- the **integrand** is implemented as an *array valued function*
 - takes an array of values : the integration points
 - returns an array of values : the function values at the integration points
- array valued functions are a F90 feature.
- The returned array is automatically allocated and deallocated
- flexible and elegant but **efficiency flaws**:
 - lots of dynamical memory management
 - function pointer **cannot be inlined** => obstructs auto-vectorization

- hardcode Gauss-Legendre integration without function pointer (two lines of code)
- elemental function allows a function that takes a scalar and returns a scalar to be applied to an array by embedding it into a vectorizable loop

```

FUNCTION Phi_integrand(ka)
  REAL (SP), INTENT(IN) :: ka(:)
  REAL (SP)              :: Phi_integrand(SIZE(ka))
  ...

```

=>

```

ELEMENTAL FUNCTION Phi_integrand(ka)
  REAL (SP), INTENT(IN) :: ka(:)
  REAL (SP)              :: Phi_integrand(SIZE(ka))
  ...

```

	runtime [s]	speedup	total speedup
original code	11.0		
optimization 1 (m_0)	4.51	2.43	2.43
optimization 2 (I/O)	3.93	1.15	2.80
vectorization	0.29	13.6	37.9

huh?

- code uses single precision and AVX (256 bit)
- vector width is 8 SP
- expected speedup of 8x from vectorization
- we gain an additional speedup of 1.7 due to removal of dynamic memory management that comes with the array valued function (integrand)
- the 0.58 s spent in I/O (optimization 2) is significant in the final code : $0.29+0.58$ is 3x slower

- only 1 core used so far
- parallelize over N cores
 - OpenMP
 - Intel TBB
 - ...
- only useful if the work load increases considerably
 - number of temperature points increases
 - single precision -> double precision (implies more iterations)
- current setup overhead would probably be larger than speedup

- think about the problem when you code
- C++ can be as efficient as Fortran (Tips & Tricks 1)
- Fortran also contains idioms that can kill performance (Fortran can be as inefficient as C++)
- constructs that get in the way of vectorization are often inefficient by themselves
 - ⇒ the speedup of vectorization can be larger than the vector width
- it pays off to let me review your code

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