HPC TNT - 1

Tips and tricks – how to efficiently parallelize your code

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1. Reduce time to solution

- Machines have limited peak performance
- 2. Solve bigger problems in the same time
 - Machines have limited amount of memory
- 3. Produce more accurate solutions
 - typically implies
 - More data, e.g. more elements, basis functions, atoms, ...
 - More computations, e.g. more detailed physics, ...
 - Both

4. ...



- Computers get faster anyway, no?
- Moore's law still holds
 - # of transistors on a chip doubles every 18 months



- Used to be equivalent to program execution speed doubles every 18 months
- Not any more ...



• Clock frequency not going up anymore



- Peak performance still increases because it is multiplied by number_of_cores
 - x threads_per_core x vector_width

CPU	GHz ×	sockets × x cores	threads per core	× vector = width	GHz x f (Gflops)	GB/s	Flops/GB SP
Harpertown	2.5	4	1	4/2	40/20	4	10
Westmere	2.26	2x6	2	4/2	217/109	8	27.8
Xeon Phi	1.24	61	4	16/8	4841/2420	160	30
Ivy Bridge	2.8	2x10	2	8/4	896/484	80	11.2



- Speed of memory increases much slower than peak performance
- 5 years ago most applications were compute bound
 - Speed ~ peak performance
- Today most applications are memory bound
 - Speed ~ peak bandwidth



- Conclusion:
 - On future CPUs the speed of a serial code will certainly not increase in pace with Moore's law
- Unless you parallelize
- 4. Keep your code's performance in pace with Moore's law and stay competetive



Overview

- Why parallelize?
- When parallelize?
- Know your goal and minimize coding effort
- Common approaches towards parallelization
- What to parallelize?
- Case study



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- When you hit the wall(s)
 - Program takes too long
 - Single node memory too small
 - Outperformed by competitor
- You need to parallelize ... Are you sure? Consider

Serial optimization Shared memory machine



When parallelize? what to do first ...

- Optimize serial code often significant speedup possible
 - Use appropriate data layouts
 - Use appropriate algorithms
 - Use good tools
 - Intel compiler suite generally better than gcc
 - Use HPC libraries
 - Prefer to extend existing codes rather reinventing the wheel
 - Look for well documented code
 - User forum traffic
 - Download counts
 - Citations
 - Compile for CPU you want to run on: -xhost -O3 [-fast]
 - Understand what influences the performance of your code

Serial optimization what influences serial performance?





- Data traffic
 - Need ~200 cycles to move data from main memory to CPU
 - Core can do 4x200 single precision operations in that time

The cost of memory Westmere node layout









The cost of memory

- UMA
 - Uniform memory access
 - Is gone
- ccNUMA
 - Cache coherent non-uniform memory access
 - Multiple copies of data
 - Mechanisms to maintain coherency
 - The farther away data is from processor, the longer it takes to fetch it
 - Complicating factor
 - It is here to stay ...
 - Overlap computation and communication
 - = form of parallelization



Serial optimization what influences serial performance?

- Vectorization = parallelization in a single thread
 - SIMD, FMA
 - Apply instruction to vector register instead of scalar register
 - Register width
 - 128 bit = 4 SP = 2 DP Harpertown, Westmere (Turing)
 256 bit = 8 SP = 4 DP Ivy Bridge (Hopper)
 - 250 bit = 8 SP = 4 DP• 512 bit = 16 SP = 8 DP

Ivy Bridge Xeon Phi (Hopper) (Vic3)

- Pipelines
 - LIO DIO XIO LI1 DI1 XI1 LI2 DI2 XI2 ...
 - 5 stage pipeline
 LI0 DI0 XI0 LI5 DI5 XI5 LI10 DI10 XI10 ...
 LI1 DI1 XI1 LI6 DI6 XI6 LI10 DI10 ...
 LI2 DI2 XI2 LI7 DI7 XI7 LI10 ...
 LI3 DI3 XI3 LI8 DI8 XI8 ...
 LI4 DI4 XI4 LI9 DI9 ...
 - Pipelines can be broken by
 - load/store from/to main memory
 - conditional branches



When to parallelize? and what to do first ...

Criteria for efficient loops – 1

Prefer loops with high computational intensity

- Number of Flops per memory access
- The higher the better
- SIMD very powerful, won't help if memory bound
- Code balance = (Computational intensity)⁻¹
- Don't cheat, measure useful work





Roofline model



Computational intensity (I) [F/B]



Roofline model



Computational intensity (I) [F/B]



Roofline model





peak performance/bandwidth = FLOPs per byte you need to keep CPU busy

• (for loops that read from main memory)

CPU	GHz	sockets x cores	threads per core	vector width	GHz x f (Gflops)	GB/s	FLOPs/B
Harpertown	2.5	4	1	4/2	40	4	10
Westmere	2.26	2x6	2	4/2	217	8	27.8
Xeon Phi	1.24	61	4	16/8	4841	160	30
Ivy Bridge	2.8	2x10	2	8/4	896	80	11.2



When to parallelize? and what to do first ...

Criteria for efficient loops – 2

Prefer loops with unit stride

```
float a[N];
for(int i=0; i<N; i+=stride) { a[i] = ... }</pre>
```

- every load/store loads/stores an entire cache line
 - typically 64 Bytes = 16 SP = 8 DP
- Avoid filling the cache with data you do not need
- Make sure you use the data that are loaded in the cache

Prefer data structures enabling unit stride

- Array of structure (AoS) vs struct Particle // AoS { double x,y,z,vx,vz,vy,m; }; Particle particles[N];
 // not efficient since // non-unit stride for loops // which do not use all
 struct Particle of arrays (SoA) struct Particles // SoA { double x[N],y[N],...; }; Particles particles;
 // efficient, also for SIMD // but mind indirect data access!
 - // properties in the struct.
 // Also bad for SIMD vectorization



The cost of memory

• Criteria for efficient loops – 3

Prefer predictable loops

• Latency can be hidden by prefetching (compiler does this)

Avoid unpredictable loops

- Conditional branches
 - Break pipelines
- Indirect addressing/Pointer chasing
 - Bad memory access patterns, many cache misses
- Compiler has no clue ...





When to parallelize? Or what to do first ...

- Cache size = 32 Kb = 4K doubles
- Cache line size is 64 bytes or 4 DP or 8 SP
 - Every read will transfer 64 bytes to L1
 - Main memory->L1 200 cycles
 - L3->L1 52 cycles
- Cache misses are expensive: you easily miss hundreds of compute cycles
- Exploit spatial and temporal data locality



When to parallelize? Or what to do first ...

- Spatial data locality =
 - make sure you use all data in a cache line don't jump around in main memory
 - > Sort data approximately in the order that you need them in loops
- Temporal data locality = once your data is in L1 cache, use it as much as possible
 - > Apply tiling



Tiling

// inefficient // efficient // except small problems // chunk = collection of items that fits in L1 cache 11 For all chunks For all items Do this For all items in chunk For all items Do this For all items in chunk Do that For all items Do that For all items in chunk Do something else Do something else

// data transferred 3x // data transferred once



When to parallelize? and what to do first ...

• Criteria for efficient loops – 4

Prefer long loops

 Amortize startup and cleanup cost of pipelines and loop overhead





Criteria for efficient loops – summary

Prefer loops which have high computational intensity have unit stride are predictable are long



The numbers tell the tale

• Know where to optimize

- Think! may be sufficient for small program
- Otherwise, measure performance using profiling tools
 - gprof
 - Llkwid-perfctr
 - PerfExpert
 - Intel Vtune
 - Allinea Map
- Hardware counters
 - # instructions
 - # cache misses
 - # memory read/writes
 - # TLB misses





Overview

- Why parallelize?
- When to parallelize?

• Know your goal and minimize coding effort

- Common approaches towards parallelization
- What to parallelize?
- Case study



Know your goal Minimize coding effort

- How much memory do you need?
- Required time to solution?
 - May include development time
- How many cpu years will your code run?
- How much time can you afford to spend on coding?
- Is anything available in open source community?
 - A few days of *googling* around may save you months of development
 - Your programming skills will improve **more** by using someone else's good code than by trying to reinvent the wheel



Overview

- Why parallelize?
- When to parallelize?
- Know your goal and minimize coding effort

• Interludium

- Common approaches towards parallelization
- What to parallelize?
- Case study





How (not) to program ...

• Lennard-Jones potential





How (not) to program ...

```
double VLJ0( double r ) {
    return 1./pow(r,12) - 1./pow(r,6);
                                                           // 18.0 x slower
}
double VLJ1( double r )_{
    return std::pow(r,-12) - std::pow(r,-6);
                                                           // 14.9 x slower
}
double VLJ2( double r ) {
    double tmp = std::pow(r,-6);
    return tmp*(tmp-1.0);
                                                            // 7.8 x slower
}
double VLJ3( double r ) {
    double tmp = 1.0/(r*r*r*r*r*r);
    return tmp*(tmp-1.0);
                                                           // 1.01 x slower
}
double VLJ( Real t r ) {
    double rr = 1./r;
    rr *= rr;
    double rr6 = rr*rr*rr;
    return rr6*(rr6-1);
                                                               // 1 x slower
}
```



Overview

- Why parallelize?
- When to parallelize?
- Know your goal and minimize coding effort
- Common approaches towards parallelization
- What to parallelize?
- Case study





Common parallelization approaches

Shared memory machine

- One global address space (not necessarily uniform)
- No (explicit) communication

Hybrid machine

- Each process manages several threads
- One global address space per process
- One process per socket, or per pair of SMT threads, ...

Distributed memory machine

- No global address space
- One process per thread
- Each process has its own address space
- Communication between processes to share data







Common parallelization approaches

Shared memory

- OpenMP (C/C++/Fortran)
- Intel TBB (C++)
- Intel cilk++ (C++)
- (Raw threads)
- (MPI) (C/C++/Fortran)
- Charm++ parallel objects (C++)
- Global Array toolkit (C/C++)

• Distributed memory

- MPI
- Charm++ parallel objects
- Global array toolkit

Hybrid

 MPI between nodes, shared memory approach in each process



Overview

- Why parallelize? Computers get faster anyway, No?
- When to parallelize? Or what to do first
- Know your goal and minimize coding effort
- Common approaches towards parallelization
- What to parallelize?
- Case study


What to parallelize?

- Communication is overhead and slow
 - Bandwidth and latency order of magnitude worse than main memory access
 - Try overlapping communication and computation
- Generally, prefer parallelizing
 - Large loops with high computational intensity
 - Tasks with little communication
 - Big chunks of code over small ones (coarse grained)
 - Chunks of a fixed load over variable loads
 - Otherwise, schedule largest tasks first





- Why parallelize?
- When to parallelize?
- Know your goal and minimize coding effort
- Common approaches towards parallelization
- What to parallelize?



• Case study – Molecular Dynamics



Test case

- Small molecular dynamics code
- Kindly provided by Jesus Eduardo Galvan Moya from Physics Department – Condensed Matter theory
- Serves many didactical (HPC) purposes
 - Simple code, not to big, easy to understand, ...
 - Full of issues you should learn to pay attention to







Case study

- Ground state energy calculation of atomistic system
- 0K, no velocities
- 10-150 atoms
- Pairwise interaction potential, brute force (no cut off)
 - 50*49/2 = 1125 pair potential evaluations
 - 150*149/2 = 11175 pair potential evaluations
- 1000 runs of 200000 atom moves (Monte Carlo samples)
- Followed by quasi-Newton method to improve the MC minimum
- Fortran90





do i_run=1,1000	in=1,1000 local minimum loop }		}	
do i_mcs=1,200000	Monte Carlo	Ιοοι	p	}
Etot=0			}	}
do i=1,n	energy loop	}	}	}
do j=i+1,n		}	}	}
$Etot = Etot + f(r_{ij})$		}	}	}
end do		}	}	}
end do		}	}	}
keep lowest energy configuration			}	}
end do			}	}
improve local minimum with quasi-new	rton			}
end do				}
keen lowest onergy configuration alabel	nainina (ha			

keep lowest energy configuration = global minimum (hopefully)



Case study memory footprint

- Problem size
 - 3 position coordinates * nAtoms * 8 bytes/coordinate
 - 50 atoms -> 1200 bytes ~ 1.2 Kb
 - 150 atoms -> 3600 bytes ~ 3.6 Kb
- Turing harpertown nodes 2 quad cores
 - 2x4=8 threads
 - L1 Cache size = 32 Kb per core
- Turing Westmere nodes 2 six cores with SMT
 - 2x6x2=24 threads
 - L1 Cache size = 32 Kb per core
- Fits in L1 cache easily, no need for tiling



Case study - optimization

- Which parts in the code need optimization?
 - Energy loop (pairs of atoms)
 - Small part of code
 - Executed most often 1125x20000x1000
 - Definitely needs optimization ("What to do first")
 - Monte Carlo loop
 - NR part represents small fraction of loop, little to be gained
 - Global minimum loop
 - Mainly just a loop





do i=1,N
ri(1) = x(i)
ri(2) = y(i)
ri(3) = z(i)
do j=i+1,N
rj(1) = x(j)
rj(2) = y(j)
rj(3) = z(j)
Etotal = Etotal + Energy(ri,rj)
end do
end do



function Energy(ra,rb)

```
!...
r=sqrt((rb(1)-ra(1))**2+(rb(2)-ra(2))**2+(rb(3)-ra(3))**2)
Energy = intpot_fitting(r)
return
```

end

```
function intpot_fitting(r)
!...
intpot_fitting = Acoeff*exp(-alpha*r)/r**npow
        - Bcoeff*exp(-beta*(r-catt))/((r-catt)**nattractive+datt)
        - 0*Ccoeff/r
return
```

end



```
function Energy(ra,rb)
1 . . .
  r=sqrt((rb(1)-ra(1))**2+(rb(2)-ra(2))**2+(rb(3)-ra(3))**2)
  Energy = intpot fitting(r)

    Both functions have high

return
                                         computational intensity
end

    Loops will be compute

function intpot fitting(r)
                                         bound
!...
  intpot fitting = Acoeff*exp(-alpha*r)/r**npow
    - Bcoeff*exp(-beta*(r-catt))/((r-catt)**nattractive+datt)
    - 0*Ccoeff/r
Return
end
                          +,-,* are cheap
                                          1 cycle
            /, exp(.), sqrt(.) are expensive
                                          ~20 cycles
```

pow(.,.) is very expensive ~100 cycles





- 50 atoms
 - Fortran version 150 µs (auto-vectorization turned off)
 - C/C++ version 144 μ s
- I am not a Fortran specialist
- Tried to optimize a C/C++ version first





- Energy loop contains two nested function calls
- Prevents C++ from vectorizing the inner loop
- Remove call to Energy, compute interatomic distance rij in loop body and call intpot_fitting
- 144->96 µs (now vectorized)



- Intpot_fitting contains division by power: Acoeff*exp(-alpha*r)/r**npow
- Equivalent to
 - Acoeff*exp(-alpha*r)*r**(-npow)
- But saves a division ~20 cycles
- 144->96->93 µs
- Only small gain because Intpot_fitting is expensive anyway (5 intrinsic function calls)





- Remove the call to intpot_fitting and compute in the body of the loop
- 144->96->93-><mark>9</mark>3 µs
- Compiler good at inlining 1 function call, not 2.



Case study Energy loop

- Inner loop runs over [i+1,N[
- So its data is not always well aligned
- Can slow down vectorization
- Let inner loop run over [0,i[
- 144->96->93->93->93 µs





- N-1 inner loops, not very long
- Split loop
 - Compute and store interatomic distance in array of length $N^*(N-1)/2 = 1225$
 - loop over atomic distance array and compute intpot_fitting in one long array instead of many short ones
- 144->96->93->93->86µs
- Criteria for efficient loops 4 Prefer long loops



```
for( int i=1, ij=0; i<N; ++i ) {// may safely skip i=1</pre>
   Real ri[3] = { x[i], y[i], z[i] };
   for( int j=0; j<i; ++j, ++ij ) {</pre>
                                                       Keep sqrt for
      r[ij] = sqrt sq(x[j]-ri[0])
                                                      computational
                   + sq(y[j]-ri[1])
                                                         intensity
                   + sq(z[j]-ri[2]) );
   }
}
Etotal = 0;
for( int ij=0; ij<N*(N-1)/2; ++ij ) {</pre>
   Etotal += Acoeff*exp(-alpha*r[ij])/pow(r[ij],npow)
            - Bcoeff*exp(-beta*(r[ij]-catt))/
                 (pow(r[ij]-catt,nattractive)+datt)
            - 0*Ccoeff/r[ij];
}
```



Case study Energy loop

- Applying the same techniques in fortran
- Auto-vectorization
- 150->95 µs
- Lower triangle and remove a division
- 150->95->88 µs
- Loop splitting
- 150->95->88-><mark>85 µs</mark>



• Same result as C++ -> confidence

- Analysis
- Programming language used
- Common misconception
 - Fortran is efficient
 - C++ is not efficient
- Rather :
 - Computational efficiency necessitates a particular programming style (stay away from high level C++ features)



Are we satisfied ...

- Speedup 95->85 µs = 1.12 ⊗
- 150 atoms (x3) -> 747µs (x8.7 ~ x3²)
- Energy loop is O(N²)
- Atoms x10 -> cputime x100 \otimes
- Alternatives?





• Understand your code!

- This Monte Carlo sampling moves only one atom at a time
- For N atoms only N-1 interatomic distances and interaction energies change instead of all N(N-1)/2
 - $N(N-1)/2 \sim N^2/2$
- Exploit this!







• Linear array containing

 $r_{10}, r_{20}, r_{21}, r_{30}, r_{31}, r_{32}, r_{40}, r_{41}, r_{42}, r_{43}, \dots$









See

Move 1 atom



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Sam

New algorithm



- More code, loops harder to optimize for compiler (shorter loops, varying stride, ...)
 - E.g. recompute loops not vectorized yet ...
 - Little hope for auto-vectorization
 - SIMD Vectorization certainly possible using Vectorization library (e.g. Vc or Boost.simd in NT²). Expect speedup x2 on Turing, x4 on Hopper
- Nontrivial code requires documentation



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What did we gain?



- Always look for O(N) algorithms if problem size is likely to grow in the future
- Always start with the simplest algorithm so you have a reference for correctness testing



Profiling with PerfExpert

- PerfExpert is a tool that combines a simple user interface with a sophisticated analysis engine to:
 - Detect and diagnose the causes for core, socket, and node-level performance issues.
 - Provide a performance analysis report and suggestions for remediation.
 - Apply pattern-based software transformations to enhance performance.



Profiling with PerfExpert

PerfExpert output of inner loop above:

Loop in function	_pow2_h9 in ~un	known-file~:0	(68.58% of the total runtime)
ratio to total instrns		. 25	50
- data accesses * GFLOPS (% max) - packed - scalar	25.4 27.3 15.2 ************************************	****	The program spends 69% evaluating std::pow(.,.) (Also 18% on std::exp(.)) These are called by $f(r_{ij})$.
performance assessment	LCPI good	okay	fairpoorbad
* overall * data accesses - L1d hits	0.58 >>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>	·>>> ·>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>	The program is compute bound (as expected).
- L2d hits - L3d hits - LLC misses	0.02 0.00 0.00		The overall performance is considered okay
 Still room for improvement? Interaction potential very expensive 2 pow, 2 exp, 1 sqrt, 3 div Still high fraction of scalar code 		e	Roughly half of the instructions is still scalar, although pow and exp are vectorized (svml prefix).
			Data fits in L1d cache (as expected).



Case study - Parallelization

- Which part in the code can be parallelized?
 - Energy loop (pairs of atoms)
 - Small part of code
 - Executed most often 1125x1000x200000
 - MC sampling loop
 - Local minimum loop
- Each can be parallelized
- Which is best?



Case study

- Approach -> OpenMP
 - Simple from programmer's point of view
- When using OpenMP always go for intel compiler suite overhead start/stop/synchronization is much larger for gcc OpenMP than for intel OpenMP
 - Intel \sim 100s of cycles
 - Gcc \sim 1000s of cycles
- There are very good alternatives to OpenMP
 - Intel Threading Building Blocks (TBB)
 - Intel Cilk++
 - (but not for Fortran)
- Disadvantage = shared memory





- Energy loop relatively short (trip count 1225) and fine grained
 - Overhead of starting and stopping OpenMP threads will kill us
 - O(N) algorithm even worse





- MC sampling loop much longer (trip count 200.000) and coarse-grained
 - Using OpenMP we should be able to run 24 threads
 - good code balance -> threads can be kept busy
 - small memory footprint -> everything can stay in cache
 - Ideal situation
 - Each thread would do 200.000/24 atom moves (and Etot computations)
 - Sufficient to amortize overhead of starting and stopping OpenMP threads
 - This leaves quasi-Newton minimization serial



Case study // global minimum loop

- Global minimum loop small trip count (1000) but very coarse grained
- Could be parallelized with OpenMP
 - Limited to single node = 24 OpenMP threads
 - time to solution is 1000/24=42 x serial execution time



Case study // global minimum loop

• Think!

- Global minimum loop iterations are completely independent – no communication between iterations
- Apply process parallelism



Case study process parallelism

- Strip outer loop from program
 - new program computes single local minimum
- Run this program 1000 times
 - Worker framework can be done with one job
 - Westmere node can run 24 instances of program simultaneously
- Use a script (python, bash) to process the output of the jobs to pick the global minimum





- Westmere nodes can run 2 threads per core (SMT)
- SMT = simultaneous multithreading
 - While thread 1 is not using some functional unit, that functional unit can be used by thread 2
 - Thread 2 "feeds on leftovers of thread 1"
 - Overlap memory traffic and instruction execution
 - Thread scheduling done by hardware
 - Speedup at most 2, usually less




- Westmere nodes can run 2 threads per core (SMT)
- Use worker framework
 - 12 threads (no SMT) 68.5 cpu seconds/thread
 - 24 threads (SMT) 96.8 cpu seconds/thread
 - Slowdown of 1.4 for 2x instances
 - Throughput x 1.42
- Time to solution for 1000 runs
 - Using 1000/24 = 42 nodes ~ 1.42 x t_serial_execution
 - Using 1000/12 = 84 nodes ~ 1.00 x t_serial_execution



Case study process parallelism

- Program parallelization only necessary if the time to solution must be less than t_serial_execution
- This comes at a cost
 - More cputime because of communication
 - Development time



Overview

- Why parallelize?
- When parallelize?
- Know your goal and minimize coding effort
- Common approaches towards parallelization
- What to parallelize?
- Case study Molecular Dynamics

• Final remarks



- Reasons to parallelize
- But, before you parallelize,
- But, before you optimize,
- Before you write code,
- In any case,

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- Optimize!
- Profile your code
- Consider reusing OS code
- Talk to us



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- If you would have to reduce time to solution, which loop would you parallelize?
 - Energy loop
 - MC sampling loop
 - Local minimum loop Loop
- Which approach would you use, ant why
 - OpenMP
 - MPI

